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Generic Related-key Attacks for HMAC

Thomas Peyrin (joint work with Yu Sasaki and Lei Wang)

Nanyang Technological University - Singapore

TCCM-CACR 2012

Chengdu, China - November 24, 2012



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Distinguish-R attack Intermediate internal state recovery Existential forgery and distinguish-H attack

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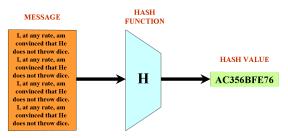
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Conclusion

What is a Hash Function ?



- *H* maps an **arbitrary length input** (the message *M*) to a **fixed length output** (typically *n* = 128, *n* = 160 or *n* = 256).
- no secret parameter.
- *H* must be easy to compute.
- examples: MD5 (1992), SHA-1 (1995), SHA-2 (2001), SHA-3 (2012)

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The security goals

pre-image resistance:

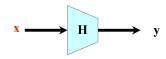
given an output challenge y, the attacker can not find a message x such that H(x) = y, in less than $\theta(2^n)$ operations.

2nd pre-image resistance:

given a challenge (x, y) so that H(x) = y, the attacker can not find a message $x' \neq x$ such that H(x') = y, in less than $\theta(2^n)$ operations.

collision resistance:

the attacker can not find two messages (x, x') such that H(x) = H(x'), in less than $\theta(2^{n/2})$ operations (a generic attack with the birthday paradox exists [Yuval-79]).



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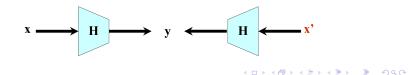
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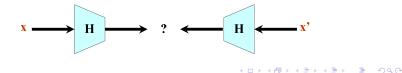
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collision resistance:

the attacker can not find two messages (x, x') such that H(x) = H(x'), in less than $\theta(2^{n/2})$ operations (a generic attack with the birthday paradox exists [Yuval-79]).

And other ones: near collisions, multicollisions, random oracle look-alike, ...

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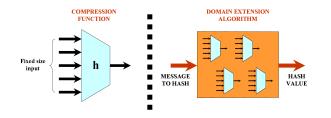
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General construction

For historical reasons, most hash functions are composed of two elements:

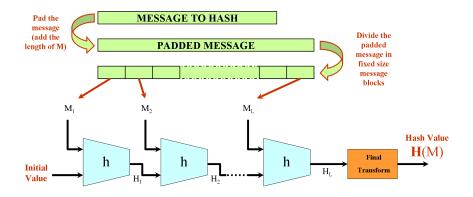
- a compression function *h*: a function for which the input and output size is fixed.
- a domain extension algorithm: an iterative process that uses the compression function *h* so that the hash function *H* can handle inputs of arbitrary length.



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The Merkle-Damgård domain extension algorithm

The most famous domain extension algorithm used is called the **Merkle-Damgård** [Merkle Damgård-89] iterative algorithm.



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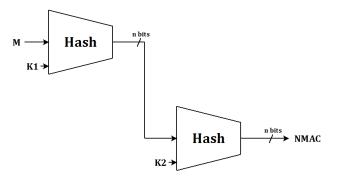
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HMAC and NMAC (Bellare et al. - 1996)

A MAC outputs an *n*-bit value from a *k*-bit key *K* and an arbitrary long message *M*.

$$NMAC(K_1, K_2, M) = H(K_2, H(K_1, M))$$



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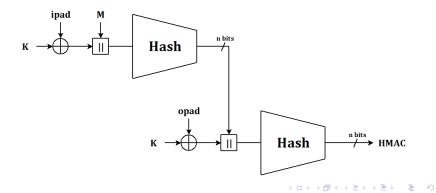
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HMAC and NMAC (Bellare et al. - 1996)

A MAC outputs an *n*-bit value from a *k*-bit key *K* and an arbitrary long message *M*.

$$extsf{HMAC}(K,M) = H(K \oplus extsf{opad} \mid\mid H(K \oplus extsf{ipad} \mid\mid M))$$



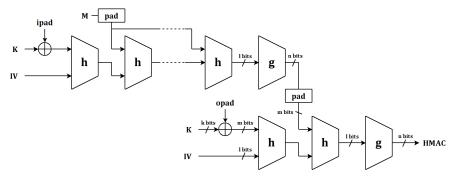
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HMAC and NMAC (Bellare et al. - 1996)

A MAC outputs an *n*-bit value from a *k*-bit key *K* and an arbitrary long message *M*.

 $\operatorname{HMAC}(K,M) = H(K \oplus \operatorname{\mathbf{opad}} || H(K \oplus \operatorname{\mathbf{ipad}} || M))$



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Universal and existential forgery

The game played:

The attacker can query an oracle, $HMAC_K$, and tries to generate a valid MAC with the key *K* for a message that he didn't query yet

When the message is chosen by the **challenger**: it is a **universal forgery**

When the message is chosen by the **attacker**: it is an **existential forgery**

HMAC: MACing with hash functions

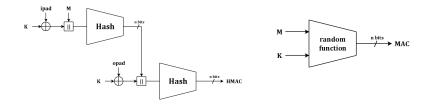
A generic related-key attack on HMAC 000000 000000 00 Conclusion

Distinguishing-R

The game played:

The attacker can query an oracle, F_K , that is instantiated either with HMAC_K, or with a random function R_K . He must obtain non-negligible advantage in distinguishing the two cases:

$$Adv(\mathcal{A}) = |\Pr[\mathcal{A}(\operatorname{HMAC}_K) = 1] - \Pr[\mathcal{A}(R_K) = 1]|.$$



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HMAC: MACing with hash functions

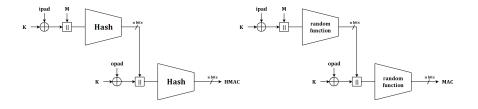
A generic related-key attack on HMAC 000000 000000 00 Conclusion

Distinguishing-H

The game played:

The attacker can query an oracle, $HMAC_K$, that is instantiated either with $HMAC_K^{H(h)}$ or with $HMAC_K^{H(r)}$, where *H* is a known dedicated hash function, *h* a known dedicated compression function, and *r* a randomly chosen function. He must obtain non-negligible advantage in distinguishing the two cases:

$$Adv(\mathcal{A}) = \left| \Pr[\mathcal{A}(\texttt{HMAC}_{K}^{H(h)}) = 1] - \Pr[\mathcal{A}(\texttt{HMAC}_{K}^{H(r)}) = 1] \right|$$



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Known dedicated attacks on HMAC

Attack	Key Setting	Target	Size	#Rounds	Comp.	Ref.
DistH	Single key	MD4	128	Full	$2^{121.5}$	[KBPH06]
DistH	Single key	MD5	128	33/64	$2^{126.1}$	[KBPH06]
DistH	Single Key	MD5	128	Full	2 ⁹⁷	[WYWZZ09]
DistH	Single key	3p HAVAL	256	Full	$2^{228.6}$	[KBPH06]
DistH	Single key	4p HAVAL	256	102/128	$2^{253.9}$	[KBPH06]
DistH	Single key	SHA0	160	Full	2 ¹⁰⁹	[KBPH06]
DistH	Single key	SHA1	160	43/80	2 ^{154.9}	[KBPH06]
DistH	Single key	SHA1	160	50/80	2 ^{153.5}	[RR08]
DistH	Related Key	SHA1	160	58/80	$2^{158.74}$	[RR08]
Inner key rec.	Single Key	MD4	128	Full	2 ⁶³	[CY06]
Inner key rec.	Single Key	SHA0	160	Full	2 ⁸⁴	[CY06]
Inner key rec.	Single Key	SHA1	64	34/80	2 ³²	[RR08]
Inner key rec.	Single Key	3p HAVAL	256	Full	2122	[LCKSH08]
Full key rec.	Single Key	MD4	128	Full	2 ⁹⁵	[FLN07]
Full key rec.	Single Key	MD4	128	Full	277	[WOK08]

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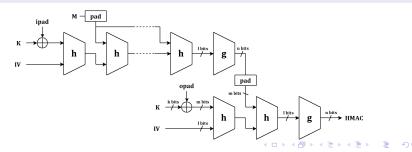
Known generic attacks on HMAC

The setting

We try to find generic attacks on HMAC with a *k*-bit when instantiated with an *n*-bit hash function using a *l*-bit internal state (with $l \le 2n$ and *k* sufficiently big to avoid brute force key recovery)

Distinguishing-H attack costs 2^{*l*} **computations (ideal)**

Universal forgery attack costs 2ⁿ computations (ideal)



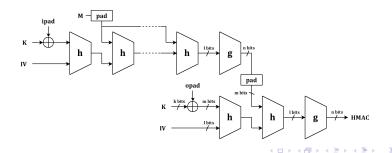
A generic related-key attack on HMAC 000000 000000 00 Conclusion

Known generic attacks on HMAC

Distinguishing-R attack costs 2^{1/2} computations (not ideal)

The procedure

- **step 1:** query $2^{l/2}$ messages and gather all pairs (M, M') that collides on the output
- step 2: for all colliding pairs, append an extra random message block M₁ and check if this new message pair (M||M₁, M'||M₁) collides as well
- step 3: if it does, the oracle implements HMAC, otherwise it is a random function



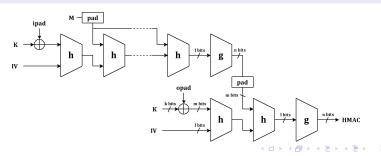
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Known generic attacks on HMAC

Existential forgery attack costs 2^{1/2} computations (not ideal)

The procedure

- **step 1:** query $2^{l/2}$ messages and gather all pairs (M, M') that collides on the output
- step 2: for all colliding pairs, append an extra random message block M₁ and check if this new message pair (M||M₁, M'||M₁) collides as well. Pick one such pair.
- **step 3:** append another extra random message block M_2 and query the MAC for message $M||M_2$. Then it is equal to the MAC for message $(M'||M_2)$



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HMAC: MACing with hash functions

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Known generic attacks on HMAC

Attack	Key Setting	Generic	
Attack	Key Setting	Complexity	
Universal forgery	Single Key	2 ⁿ	
Existential forgery	Single Key	$2^{l/2}$	
DistR	Single Key	$2^{l/2}$	
DistH	Single Key	2^l	

HMAC: MACing with hash functions

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Known generic attacks on HMAC

Attack	Key Setting	Generic	
Attack	Key Setting	Complexity 2^n ? $2^{l/2}$? $2^{l/2}$?	
Universal forgery	Related Key	2^{n} ?	
Existential forgery	Related Key	2 ^{1/2} ?	
DistR	Related Key	$2^{l/2}$?	
DistH	Related Key	2^{l} ?	

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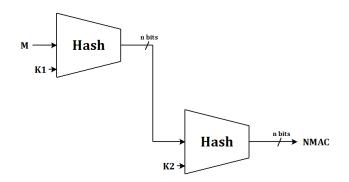
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Conclusion

What weakness to attack ?





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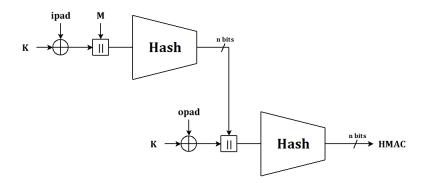
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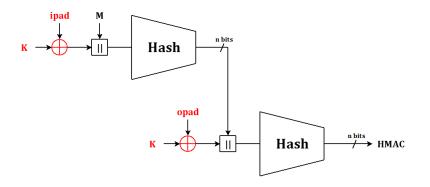


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What weakness to attack ?

HMAC (with key K)

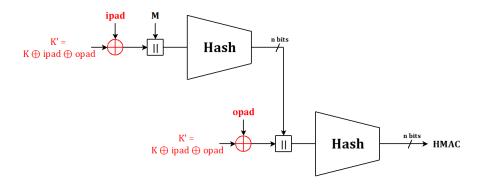


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What weakness to attack ?



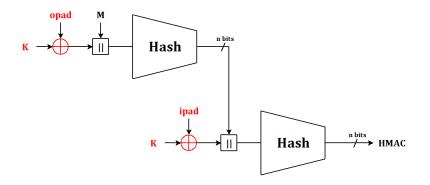


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What weakness to attack ?



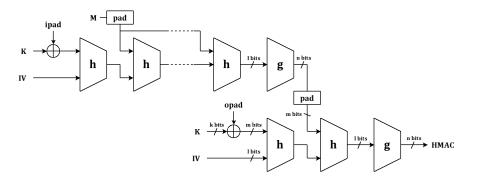


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HMAC: MACing with hash functions 00 0000 00000 Conclusion

What to detect?

HMAC (with key *K* and arbitrary message)

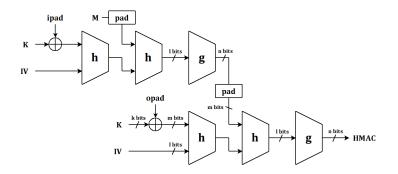


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What to detect?

HMAC (with key *K* and *n*-bit message)



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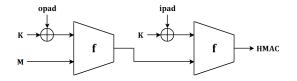
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Conclusion

What to detect ?

HMAC (with key *K* and *n*-bit message)

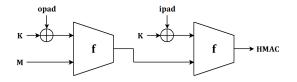


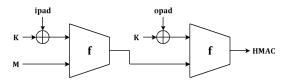
HMAC: MACing with hash functions

Conclusion

What to detect?

HMAC (with K and $K' = K \oplus ipad \oplus opad$ and *n*-bit message)



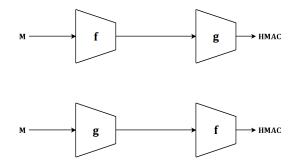


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What to detect?

HMAC (with K and $K' = K \oplus ipad \oplus opad$ and *n*-bit message)



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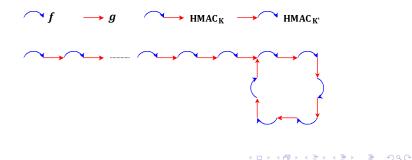
HMAC: MACing with hash functions

Conclusion

What to detect?

Functions f(g(x)) and g(f(x)) have a particular cycle structure:

there is a 1-to-1 correspondence between cycles of f(g(x)) and g(f(x))

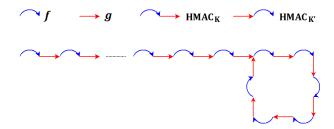


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Conclusion

How to detect the cycle structure ?

\implies by measuring cycles length



The game played (distinguishing-R in the related-key model):

The attacker can query two oracles, F_K and $F_{K'}$, that are instantiated either with HMAC_K and HMAC_{K'}, or with two independent random functions R_K and $R_{K'}$. He must obtain non-negligible advantage in distinguishing the two cases:

 $Adv(\mathcal{A}) = |\Pr[\mathcal{A}(\texttt{HMAC}_K, \texttt{HMAC}_{K'}) = 1] - \Pr[\mathcal{A}(R_K, R_{K'}) = 1]|$

HMAC: MACing with hash functions

Conclusion

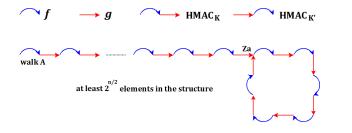
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The attack

First step (walk A)

Start from an *n*-bit random input message, query F_{K} , and keep querying as new message the MAC just received. Continue so for about $2^{n/2} + 2^{n/2-1}$ queries until getting a collision among the MACs received.

If no collision is found, or if the collision occurred in the $2^{n/2}$ first queries, the attacker outputs 0.

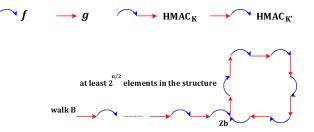


HMAC: MACing with hash functions 00 00000 000000 Conclusion

The attack

Second step (walk B)

Do the same for oracle $F_{K'}$.



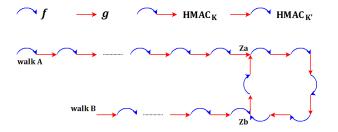
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HMAC: MACing with hash functions 00 00000 000000 Conclusion

The attack

Third step (colliding walk A and walk B)

If the cycle of walk A has the same length as the one from walk B, then output 1. Otherwise output 0.



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A generic related-key attack on HMAC

Results - distinguishing-R for HMAC with wide-pipe

The advantage of the attacker is non-negligible and **the complexity of the distinguisher** is about $2^{n/2} + 2^{n/2-1}$ computations for each of the first and second phase, thus **about** $2^{n/2+1}$ **computations in total**.

We implemented and verified the distinguisher. With SHA-2 truncated to 32 bits, we found two walks A and B that have the same cycle length of 79146 elements with 2¹⁷ computations. The best previously known attack for HMAC instantiated with SHA-2 truncated to 32 bits required 2¹²⁸ computations.

Attack	Key Setting	Target	Old Generic Complexity	New Generic Complexity	
DistR	Related Key	Wide-pipe	2 ^{<i>l</i>/2}	$2^{n/2+1}$	

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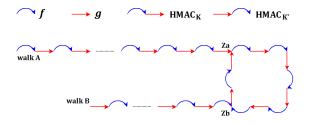
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How to recover the intermediate internal state?

We would like to know some of the intermediate internal state of ${\tt HMAC}_K$ and ${\tt HMAC}_{K'}$

Inside a colliding cycle for $HMAC_K$ and $HMAC_{K'}$, the input or output queries to $HMAC_K$ are intermediate internal state of $HMAC_{K'}$ (and vice-versa) ... but we don't know which one it is, so we need to synchronize the cycles



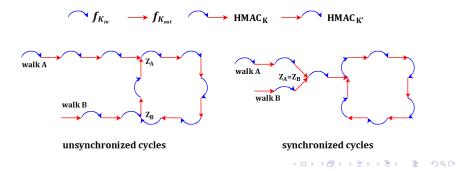
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Synchronized and Unsynchronized cycles

There are two cases for a collision between walk A and walk B:

- collision in the tail
- collision in the cycle

If the collision happens in the tail, then the cycles are directly synchronized



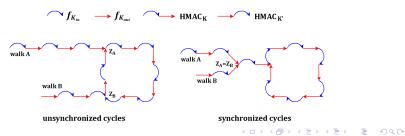
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Synchronized and Unsynchronized cycles

We just build walk A and walk B with a tail long enough, such that the collision is likely to happen in the tail.

The procedure

- **step 1 (build walk A):** same as before, but just ensure that tail in walk A has size at least $2^{n/2-2}$
- step 2 (build walk B): same as step 1, but with queries to K' = K ⊕ ipad ⊕ opad
- **step 3:** check if the cycle have the same length, and if so, there is a good chance that it happened in the tail. Then you can recover the intermediate internal states.



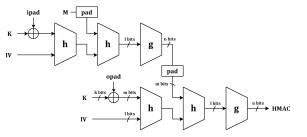
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Internal state recovery for wide-pipe

For a wide-pipe hash, the attack is not over, because we have to revert the output truncation function from the intermediate internal state and recover all *l* bits.

The procedure

- step 1: obtain an intermediate internal state
- step 2: find a collision by doing query with one extra block of random data
- **step 3:** go through all the 2^{*l*-*n*} candidates and check offline which one would have give you this collision



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Results - internal state recovery for HMAC

The complexity of the internal state recovery is about $2^{n/2+2}$ queries and 2^{l-n+1} computations in total.

Attack	Key Setting	Target	Old Generic Complexity	New Generic Complexity	
DistR	Related Key	Wide-pipe	$2^{l/2}$	$2^{n/2+1}$	
Inner state rec.	Related Key	Narrow or Wide	2^n	$2^{n/2+2} + 2^{l-n+1}$	

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Existential forgery and distinguish-H attack

- once we have recovered an internal state, forging a valid MAC is easy
- if we can recover an internal state, then distinguish-H is easy

The **complexity to forge a valid MAC or distinguish-H** is the complexity of the internal state recovery $(2^{n/2+2} + 2^{l-n+1} \text{ computations})$

Attack	Key Setting	Targat	Old Generic	New Generic	
Allack	Key Setting	Target	Complexity	Complexity	
DistR	Related Key	Wide-pipe	$2^{l/2}$	$2^{n/2+1}$	
Inner state rec.	Related Key	Narrow or Wide	2^n	$2^{n/2+2} + 2^{l-n+1}$	
Ex. forgery	Related Key	Wide-pipe	$2^{l/2}$	$2^{n/2+2} + 2^{l-n+1}$	
DistH	Related Key	Narrow or Wide	2^l	$2^{n/2+2} + 2^{l-n+1}$	

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Our results

Our attacks on HMAC work when the key has length m, or m - 1 because ipad = $0x3636 \cdots 36$ and $opad = 0x5C5C \cdots 5C$

\Longrightarrow The choice of <code>ipad</code> and <code>opad</code> was in fact important

Attack	Key Setting	Targat	Old Generic	New Generic	
Allack	Key Setting	Target	Complexity	Complexity	
DistR	Related Key	Wide-pipe	$2^{l/2}$	$2^{n/2+1}$	
Inner state rec.	Related Key	Narrow or Wide	2 ⁿ	$2^{n/2+2} + 2^{l-n+1}$	
Ex. forgery	Related Key	Wide-pipe	$2^{l/2}$	$2^{n/2+2} + 2^{l-n+1}$	
DistH	Related Key	Narrow or Wide	2^l	$2^{n/2+2} + 2^{l-n+1}$	

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Patching HMAC

1st try:

We use a different IV for the hash function in the inner and outer call but that would require to change the *H* definition and implementations

2nd try:

We truncate the HMAC output ...

... but having a smaller output reduces the expected security

Our solution:

Just **prepend a "0" bit to the message** *M*:

- no more possible for the attacker to synchronize the computation chains: the inner and outer function are made distinct
- no need to change the specification of *H*, even better: can be done on top of HMAC implementations
- almost zero performance drop

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Thank you for your attention !